

## DERIVADAS

<b>TABLA DE DERIVADAS</b>	
$y = C$	$y' = 0$
$y = f(x)^n$	$y' = n f(x)^{n-1} f'(x)$
$y = f(x) \pm g(x)$	$y' = f'(x) \pm g'(x)$
$y = c \cdot f(x)$	$y' = c \cdot f'(x)$
$y = f(x) \cdot g(x)$	$y = f'(x) \cdot g(x) + g'(x) \cdot f(x)$
$y = \frac{f(x)}{g(x)}$	$y = \frac{f'(x) \cdot g(x) - g'(x) \cdot f(x)}{g(x)^2}$
$y = \sqrt[n]{f(x)}$	$y' = \frac{1}{n \sqrt[n]{f(x)^{n-1}}} \cdot f'(x)$
$y = L f(x)$	$y' = \frac{1}{f(x)} \cdot f'(x)$
$y = e^{f(x)}$	$y = e^{f(x)} \cdot f'(x)$
$y = a^{f(x)}$	$y' = a^{f(x)} \cdot f'(x) \cdot \ln a$
$y = \operatorname{sen} f(x)$	$y' = \cos f(x) \cdot f'(x)$
$y = \cos f(x)$	$y' = -\operatorname{sen} f(x) \cdot f'(x)$
$y = \operatorname{tg} f(x)$	$y' = \frac{1}{\cos^2 f(x)} \cdot f'(x)$
$y = \operatorname{cotg} f(x)$	$y' = \frac{-1}{\operatorname{sen}^2 f(x)} \cdot f'(x)$
$y = \operatorname{arc sen} f(x)$	$y' = \frac{1}{\sqrt{1 - f(x)^2}} \cdot f'(x)$
$y = \operatorname{arc cos} f(x)$	$y' = \frac{-1}{\sqrt{1 - f(x)^2}} \cdot f'(x)$
$y = \operatorname{arc tg} f(x)$	$y' = \frac{1}{1 + f(x)^2} \cdot f'(x)$
$y = \operatorname{arc cotg} f(x)$	$y' = \frac{-1}{1 + f(x)^2} \cdot f'(x)$

1.  $y = 5x^6 - 3x^5 + 3x^3 - 2$

2.  $y = x^4 + 2x^3 + x - 4$

3.  $y = 3x^{10} + 2\sqrt{x} + \frac{3}{x}$

4.  $y = \sqrt{3} \cdot x^3 - \pi \cdot x + \sqrt{3}$

5.  $y = 4 \operatorname{sen} x - 3 \cos x$

6.  $y = 2\sqrt{x} + \frac{2}{x} + x^5$

7.  $y = 4x^3 + 2x^3 - x^3 + 4$

8.  $y = \frac{\pi}{2} \cdot \cos x - 3\sqrt{x}$

9.  $y = \cos(3x)$

10.  $y = \cos^2(x^3)$

11.  $y = \operatorname{sen}(3x^2 - 2x)$

12.  $y = \cos(x^2)$

13.  $y = \operatorname{sen}^3(2x^2)$

14.  $y = \cos^4(3x^4)$

15.  $y = 3 \operatorname{sen}^2(2x - 3)$

16.  $y = \cos^5(3x^2)$

17.  $y = \cos(\operatorname{sen} x)$

18.  $y = \cos^2(\operatorname{sen}(3x))$

19.  $y = \sqrt[3]{\cos^2 x}$

20.  $y = \sqrt[3]{\cos^2(x^2)}$

21.  $y = \sqrt{x^2 - 3x}$

22.  $y = \sqrt[3]{(x^2 - 3x)^2}$

23.  $y = (2\sqrt{x} - 3x)^3$

24.  $y = \sqrt[3]{\operatorname{sen}^2 x}$

25.  $y = \sqrt[5]{\operatorname{sen}(3x)}$

26.  $y = \sqrt{3x - \operatorname{sen} x}$

27.  $y = (3x^2 - \sqrt{1-x^2})^3$

28.  $y = \operatorname{sen}\left(\sqrt{3x^2 - 5x}\right)$

29.  $y = \sqrt{\operatorname{sen}^3 x + (x-1)^3}$

30.  $y = \cos^3\left(x^2 - 3\sqrt{x}\right)$

31.  $y = \frac{x}{5}$

32.  $y = \frac{5}{x}$

33.  $y = \frac{x^4 - 3x}{4}$

34.  $y = \frac{x^3 - 3}{x}$

35.  $y = \frac{(x^4 - 3x)^2}{3}$

36.  $y = \frac{(x-1)^3}{3x}$

37.  $y = \frac{x^2}{x^2 - 1}$

38.  $y = \frac{\sqrt{3x}}{x}$

39.  $y = \sqrt{\frac{3}{x}}$

40.  $y = \frac{x}{\sqrt{3x}}$

41.  $y = \sqrt[3]{3x^2 - \operatorname{sen} x}$

42.  $y = \ln(3x - 1)$

43.  $y = \ln(x^2 - 3x)$

44.  $y = \ln \sqrt{x-2}$

45.  $y = \log_2(3x^2)$

46.  $y = e^{x^2}$

47.  $y = 2^x$

48.  $y = e^{x^2-2x}$

49.  $y = 3^{\operatorname{sen} x}$

50.  $y = \operatorname{tg}(x^3)$

51.  $y = 3e^{x^2-3x}$

52.  $y = \sqrt{e^{\cos x}}$

53.  $y = 3 \operatorname{tg}^2 x$

54.  $y = (x^2 - 1) \cdot (x - 1)$

55.  $y = x^2 \cdot \ln x$

56.  $y = e^{x^2} \cdot \cos x$

57.  $y = x^4 \cdot e^{3x}$

58.  $y = e^{x^4-3x^2} \cdot \operatorname{sen} x$

59.  $y = \ln x^2 \cdot e^{\operatorname{sen} x}$

60.  $y = \frac{1}{\ln \sqrt{x}}$

61.  $y = \left( \frac{x^2 - 3}{x^2 + 1} \right)^3$

62.  $y = \ln x \cdot e^{x^2-\operatorname{sen} x}$

63.  $y = (\cos^2 3x - \operatorname{sen}^3 x) \cdot e^{x^3}$

64.  $y = \left( \frac{\ln x^2}{x^3 - 2} \right)^2$

65.  $y = \frac{\ln x}{3^x}$

66.  $y = \frac{e^x + \ln x}{x^2 - \operatorname{sen} x}$

67.  $y = \ln \left( \frac{\operatorname{sen} x}{e^x} \right)$

68.  $y = \sqrt{\frac{\operatorname{sen} x}{x - 1}}$

69.  $y = \frac{3x^4 - 2x^2 + 3x - 2}{2x - 1}$

70.  $y = (\operatorname{sen}(e^{3x}))^2 \cdot \cos x$

71.  $y = \operatorname{arctg}(x^2)$

72.  $y = \operatorname{arcse}n x^3$

73.  $y = \ln(\sec x)$

74.  $y = \operatorname{arctg}(\ln x)$

75.  $y = \operatorname{arcse}n x \cdot e^{\cos x}$

76.  $y = \operatorname{arctg}(e^{3x})$

77.  $y = \ln\left(\frac{\operatorname{tg}x}{e^{3x^2}}\right)$

78.  $y = \operatorname{arc sen}\left(\frac{x+1}{e^x}\right)$

79.  $y = \ln(\operatorname{arctg}(5x))$

80.  $y = \operatorname{arctg}\sqrt{x^3}$

81.  $y = 5 \operatorname{arctg}^2(\operatorname{sen}x)$

82.  $y = 3^{\operatorname{arctg}(x^2)}$

83.  $y = \frac{\operatorname{arc sen}(3x-2)}{x^2}$

84.  $y = \frac{\operatorname{sen}x - \operatorname{tg}x}{\sqrt{4x-3}}$

85.  $y = x^{\operatorname{sen}x}$

86.  $y = (\operatorname{sen}x)^{x^2}$

87.  $y = (\cos x)^{x^3-x}$

88.  $y = 4^{\operatorname{arctg}(\ln x)}$

89.  $y = \ln\left(\frac{x+2}{x^2}\right)^3$

90.  $y = \left(\frac{e^{3x}}{\operatorname{sen}x}\right)^{x^2}$

91.  $y = 10^{\left(\frac{\operatorname{sen}x-e^x}{3x-\operatorname{cos}x}\right)}$

92.  $y = \cos\left(\frac{\operatorname{tg}\sqrt{x}}{\operatorname{sen}(\ln x)}\right)$

93.  $y = \frac{x^{\operatorname{cos}x}}{(\ln x)^3}$

94.  $y = \cos^2(4e^x) \cdot \ln\left(\frac{\operatorname{tg}x}{3^{x^2}}\right)$

95.  $y = \sqrt[3]{\frac{\operatorname{sen}^2(e^x)}{\operatorname{arctg}(\operatorname{cos}x)}}$

96.  $y = \sqrt{\frac{e^{\ln(\operatorname{cos}x)}}{5^{\operatorname{cos}x}}}$

97.  $y = \frac{\sqrt{\operatorname{cos}(e^x) \cdot x}}{\sqrt{e^{\operatorname{tg}x}}}$

98.  $y = (\operatorname{tg}(e^x) + x^2)^x$

99.  $y = \sqrt{\frac{\operatorname{arctg}e^x \cdot \operatorname{cos}x}{\ln(x^2-x)}}$

100.  $y = \frac{\ln\sqrt{\operatorname{cos}x}}{\operatorname{sen}(e^{\operatorname{cos}x})}$

**SOLUCIONES SIN SIMPLIFICAR**

1.  $y' = 30x^5 - 15x^4 + 9x^2$

2.  $y' = -4x^{-5} - 6x^{-4} + 1$

3.  $y' = 30x^9 + \frac{1}{\sqrt{x}} - \frac{3}{x^2}$

4.  $y' = 3\sqrt{3} \cdot x^2 - \pi$

5.  $y' = 4 \cos x + 3 \sin x$

6.  $y' = \frac{1}{\sqrt{x}} - \frac{2}{x^2} + 5x^4$

7.  $y' = 15x^2$

8.  $y' = -\frac{\pi}{2} \sin x - \frac{3}{2\sqrt{x}}$

9.  $y' = -3 \sin(3x)$

10.  $y' = -2 \cos(x^3) \cdot \sin(x^3) \cdot 3x^2$

11.  $y' = \cos(3x^2 - 2x) \cdot (6x - 2)$

12.  $y' = -\sin(x^2) \cdot 2x$

13.  $y' = 3 \sin^2(2x^2) \cdot \cos(2x^2) \cdot 4x$

14.  $y' = 4 \cos^3(3x^4) \cdot (-\sin(3x^4)) \cdot 12x^3$

15.  $y' = 6 \sin(2x - 3) \cdot \cos(2x - 3) \cdot 2$

16.  $y' = 5 \cos^4(3x^2) \cdot (-\sin(3x^2)) \cdot 6x$

17.  $y' = -\sin(\sin x) \cdot \cos x$

18.  $y' = 2 \cos(\sin 3x) \cdot (-\sin(\sin 3x)) \cdot \cos 3x \cdot 3$

19.  $y' = \frac{-2 \cos x \cdot \sin x}{3 \sqrt[3]{\cos^4 x}}$

20.  $y' = \frac{-2 \cos(x^2) \cdot \sin(x^2) \cdot 2x}{3 \sqrt[3]{\cos^4(x^2)}}$

21.  $y' = \frac{2x - 3}{2 \sqrt{x^2 - 3x}}$

22.  $y' = \frac{2(x^2 - 3x)(2x - 3)}{3 \sqrt[3]{(x^2 - 3x)^4}}$

23.  $y' = 3 \left( 2\sqrt{x} - 3x \right)^2 \cdot \left( \frac{1}{\sqrt{x}} - 3 \right)$  24.  $y' = \frac{2 \sin x \cos x}{3 \sqrt[3]{\sin^4 x}}$

25.  $y' = \frac{3 \cos 3x}{5 \sqrt[5]{\sin^4(3x)}}$

26.  $y' = \frac{3 - \cos x}{2 \sqrt{3x - \sin x}}$

27.  $y' = 3 \left( 3x^2 - \sqrt{1-x^2} \right)^2 \cdot \left( 6x - \frac{-2x}{2 \sqrt{1-x^2}} \right)$

28.  $y' = \cos\left(\sqrt{3x^2 - 5x}\right) \cdot \frac{6x - 5}{2 \sqrt{3x^2 - 5x}}$

29.  $y' = \frac{3 \sin^2 x \cos x + 3(x-1)^2}{2 \sqrt{\sin^3 x + (x-1)^3}}$

30.  $y' = -3 \cos^2\left(x^2 - 3\sqrt{x}\right) \cdot \sin\left(x^2 - 3\sqrt{x}\right) \cdot \left(2x - \frac{3}{2\sqrt{x}}\right)$

31.  $y' = \frac{1}{5}$

32.  $y = -\frac{5}{x^2}$

33.  $y' = \frac{4x^3 - 3}{4}$

34.  $y' = 2x + \frac{3}{x^2}$

35.  $y' = \frac{2(x^4 - 3x)^2 \cdot (4x^3 - 3)}{3}$

36.  $y' = \frac{3(x-1)^2 \cdot 3x - 3(x-1)^3}{(3x)^2}$

37.  $y' = \frac{2x(x^2 - 1) - x^2 \cdot 2x}{(x^2 - 1)^2}$

38.  $y' = \frac{\frac{3}{2\sqrt{3x}} \cdot x - \sqrt{3x}}{x^2}$

39.  $y' = \frac{1}{2\sqrt[3]{\frac{3}{x}}} \cdot \frac{-3}{x^2}$

40.  $y' = \frac{\sqrt{3x} - x \frac{3}{2\sqrt{3x}}}{3x}$

41.  $y' = \frac{6x - \cos x}{3\sqrt[3]{(3x^2 - \sin x)^2}}$

42.  $y' = \frac{3}{3x - 1}$

43.  $y' = \frac{2x - 3}{x^2 - 3x}$

44.  $y' = \frac{1}{\frac{2\sqrt{x-2}}{\sqrt{x-2}}}$

45.  $y' = \frac{6x}{3x^2 \cdot \ln 2}$

46.  $y' = e^{x^2} \cdot 2x$

47.  $y' = 2^x \cdot \ln 2$

48.  $y' = e^{x^2-2x} \cdot (2x-2)$

49.  $y' = 3^{\sin x} \cdot \cos x \cdot \ln 3$

50.  $y' = \frac{3x^2}{\cos^2(x^3)}$

51.  $y' = 3e^{x^2-3x} \cdot (2x-3)$

52.  $y' = \frac{-e^{\cos x} \sin x}{2\sqrt{e^{\cos x}}}$

53.  $y' = \frac{6 \operatorname{tg} x}{\cos^2 x}$

54.  $y = 2x(x-1) + (x^2 - 1)$

55.  $y' = 2x \cdot \ln x + \frac{x^2}{x}$

56.  $y' = e^{x^2} \cdot 2x \cos x - e^{x^2} \sin x$

57.  $y' = 4x^3 \cdot e^{3x} + x^4 \cdot e^{3x} \cdot 3$

58.  $y' = e^{x^4-3x^2} \cdot (4x^3 - 6x) \sin x + e^{x^4-3x^2} \cos x$

59.  $y' = \frac{2x}{x^2} \cdot e^{\operatorname{sen} x} + \ln x^2 e^{\operatorname{sen} x} \cos x$       60.  $y' = \frac{1}{\frac{\sqrt{x}}{(\ln \sqrt{x})^2}}$

61.  $y' = 3 \left( \frac{x^2 - 3}{x^2 + 1} \right)^2 \cdot \frac{2x(x^2 + 1) - (x^2 - 3)2x}{(x^2 + 1)^2}$

62.  $y' = \frac{1}{x} \cdot e^{x^2 - \operatorname{sen} x} + \ln x \cdot e^{x^2 - \operatorname{sen} x} (2x - \cos x)$

63.  $y' = (2 \cos 3x (-\operatorname{sen} 3x) 3 - 3 \operatorname{sen}^2 x \cos x) \cdot e^{x^3} + (\cos^2 3x - \operatorname{sen}^3 x) e^{x^3} 3x^2$

64.  $y' = 2 \left( \frac{\ln x^2}{x^3 - 2} \right) \cdot \frac{\frac{2x}{x^2} (x^3 - 2) - \ln x^2 3x^2}{(x^3 - 2)^2}$

65.  $y' = \frac{\frac{1}{x} 3^x - \ln x 3^x \ln 3}{(3^x)^2}$       66.  $y' = \frac{\left( e^x + \frac{1}{x} \right) (x^2 - \operatorname{sen} x) - (e^x + \ln x) (2x - \cos x)}{(x^2 - \operatorname{sen} x)^2}$

67.  $y' = \frac{e^x}{\operatorname{sen} x} \frac{\cos x e^x - e^x \operatorname{sen} x}{(e^x)^2}$       68.  $y' = \frac{1}{2 \sqrt{\frac{\operatorname{sen} x}{x - 1}}} \cdot \frac{\cos x (x - 1) - \operatorname{sen} x}{(x - 1)^2}$

69.  $y' = \frac{(12x^3 - 4x + 3)(2x - 1) - (3x^4 - 2x^2 + 3x - 2) \cdot 2}{(2x - 1)^2}$

70.  $y' = 2 \left( \operatorname{sen}(e^{3x}) \right) \cdot \cos(e^{3x}) \cdot e^{3x} 3 \cos x - (\operatorname{sen}(e^{3x}))^2 \cdot \operatorname{sen} x$

71.  $y' = \frac{2x}{1 + x^4}$       72.  $y' = \frac{3x^2}{\sqrt{1 - x^6}}$

73.  $y' = \frac{\operatorname{sen} x}{\frac{\cos^2 x}{\sec x}}$       74.  $y' = \frac{\frac{1}{x}}{1 + (\ln x)^2}$

75.  $y' = \frac{e^{\cos x}}{\sqrt{1 - x^2}} - \arcsen x \cdot e^{\cos x} \operatorname{sen} x$       76.  $y' = \frac{e^{3x} \cdot 3}{1 + (e^{3x})^2}$

$$77. y' = \frac{e^{3x^2}}{\operatorname{tg} x} \cdot \frac{\frac{e^{3x^2}}{\cos^2 x} - \operatorname{tg} x e^{3x^2} \cdot 6x}{(e^{3x^2})^2}$$

$$78. y' = \frac{\frac{e^x - (x+1)e^x}{(e^x)^2}}{\sqrt{1 - \left(\frac{x+1}{e^x}\right)^2}}$$

$$79. y' = \frac{1}{\operatorname{arctg}(5x)} \frac{5}{1 + (5x)^2}$$

$$80. y' = \frac{\frac{3x^2}{2\sqrt{x^3}}}{1 + x^3}$$

$$81. y' = 10 \operatorname{arctg}(\operatorname{sen} x) \frac{\cos x}{1 + \operatorname{sen}^2 x}$$

$$82. y' = 3^{\operatorname{arctg}(x^2)} \frac{2x}{1 + x^4} \ln 3$$

$$83. y' = \frac{\frac{3x^2}{\sqrt{1-(3x-2)^2}} - \operatorname{arcse}n(3x-2) \cdot 2x}{x^4}$$

$$84. y' = \frac{\left(\cos x - \frac{1}{\cos^2 x}\right) \sqrt{4x-3} - (\operatorname{sen} x - \operatorname{tg} x) \frac{4}{2\sqrt{4x-3}}}{4x-3}$$

$$85. y' = \left( \cos x \cdot \ln x + \frac{\operatorname{sen} x}{x} \right) \cdot x^{\operatorname{sen} x}$$

$$86. y' = \left( 2x \ln(\operatorname{sen} x) + \frac{x^2 \cos x}{\operatorname{sen} x} \right) (\operatorname{sen} x)^{x^2}$$

$$87. y = \left( (3x^2 - 1) \ln \cos x - \frac{(x^3 - x) \operatorname{sen} x}{\cos x} \right) \cdot (\cos x)^{x^3-x}$$

$$88. y' = 4^{\operatorname{arctg}(\ln x)} \cdot \frac{x}{1 + (\ln x)^2} \cdot \ln 4$$

$$89. y' = \frac{1}{\left(\frac{x+2}{x^2}\right)^3} \cdot 3 \left(\frac{x+2}{x^2}\right)^2 \cdot \frac{x^2 - 2x(x+2)}{x^4}$$

$$90. \quad y' = \left( 2x \ln x \left( \frac{e^{3x}}{\sin x} \right) + x^2 \frac{\sin x}{e^{3x}} \frac{3e^{3x} \sin x - e^{3x} \cos x}{\sin^2 x} \right) \cdot \left( \frac{e^{3x}}{\sin x} \right)^{x^2}$$

$$91. \quad y' = 10 \left( \frac{\sin x - e^x}{3x - \cos x} \right) \cdot \ln 10 \frac{(cos x - e^x)(3x - cos x) - (\sin x - e^x)(3 + \sin x)}{(3x - \cos x)^2}$$

$$92. \quad y' = -\sin \left( \frac{\tan \sqrt{x}}{\sin(\ln x)} \right) \cdot \frac{\frac{1}{\cos^2 \sqrt{x}} \cdot \frac{1}{2\sqrt{x}} \cdot \sin(\ln x) - \tan \sqrt{x} \cdot \cos(\ln x) \cdot \frac{1}{x}}{\sin^2(\ln x)}$$

$$93. \quad y' = \frac{\left( -\sin x \ln nx + \frac{\cos x}{x} \right) x^{\cos x} (\ln x)^3 - x^{\cos x} 3 (\ln x)^2 \frac{1}{x}}{(\ln x)^6}$$

94.

$$y' = 2 \cos(4e^x) \cdot (-\sin(4e^x)) \cdot 4e^x \cdot \ln \left( \frac{\tan x}{3^{x^2}} \right) + \cos^2(4e^x) \cdot \frac{3^{x^2}}{\tan x} \frac{\frac{3^{x^2}}{\cos^2 x} - \tan x \cdot 3^{x^2} \cdot 2x \cdot \ln 3}{(3^{x^2})^2}$$

$$95. \quad y = \frac{1}{2 \sqrt[2]{\frac{e^{\ln(\cos x)}}{5^{\cos x}}}} \cdot \frac{e^{\ln(\cos x)} \frac{-\sin x}{\cos x} \cdot 5^{\cos x} - e^{\ln(\cos x)} \cdot 5^{\cos x} (-\sin x) \ln 5}{(5^{\cos x})^2}$$

96.

$$y' = \frac{1}{3 \sqrt[3]{\frac{\sin^2(e^x)}{\arctg(\cos x)}}} \cdot \frac{2 \sin(e^x) \cdot \cos(e^x) \cdot e^x \cdot \arctg(\cos x) - \sin^2(e^x) \cdot \frac{1}{1 + \cos^2 x} \cdot (-\sin x)}{\arctg^2(\cos x)}$$

$$97. \quad y' = \frac{\frac{-\sin(e^x) e^x x + \cos(e^x)}{\sqrt{\cos(e^x) \cdot x}} \cdot \sqrt{e^{\tan x}} - \sqrt{\cos(e^x) \cdot x} \cdot \frac{1}{2 \sqrt{e^{\tan x}}} \cdot e^{\tan x} \cdot \frac{1}{\cos^2 x}}{e^{\tan x}}$$

$$98. \quad y' = \left( \ln(tg e^x + x^2) + x \frac{\frac{e^x}{\cos^2(e^x)} + 2x}{tge^x + x^2} \right) \cdot (tg(e^x) + x^2)^x$$

99.

$$y' = \frac{1}{2 \sqrt{\frac{\arctg e^x \cdot \cos x}{\ln(x^2 - x)}}} \cdot \frac{\left( \frac{e^x}{1 + (e^x)^2} \cos x - \arctg e^x \sin x \right) \ln(x^2 - x) - (\arctg e^x \cos x) \frac{2x - 1}{x^2 - x}}{\ln^2(x^2 - x)}$$

$$100. \quad y' = \frac{\frac{1}{\sqrt{\cos x}} \frac{-\sin x}{2 \sqrt{\cos x}} \sin(e^{\cos x}) - \ln \sqrt{\cos x} \cos(e^{\cos x}) e^{\cos x} (-\sin x)}{\sin^2(e^{\cos x})}$$